



# Universal Solutions in Temporal Data Exchange

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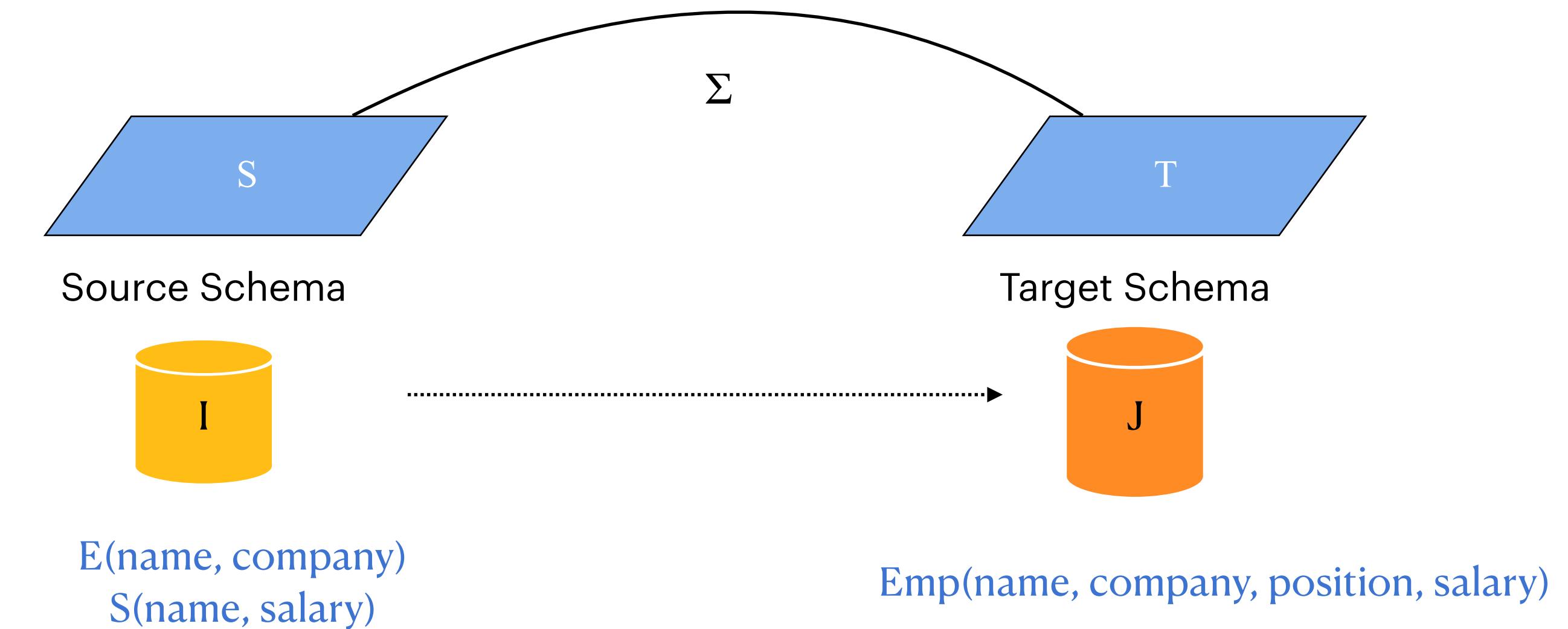
24 September 2020

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Transform data structured under a source schema into data structured under a different target schema.

**Schema Mapping**  $\mathcal{M} = (S, T, \Sigma)$

- Relational **source** schema **S**, Relational **target** schema **T**
- A set  $\Sigma$  of constraints between **S** and **T**



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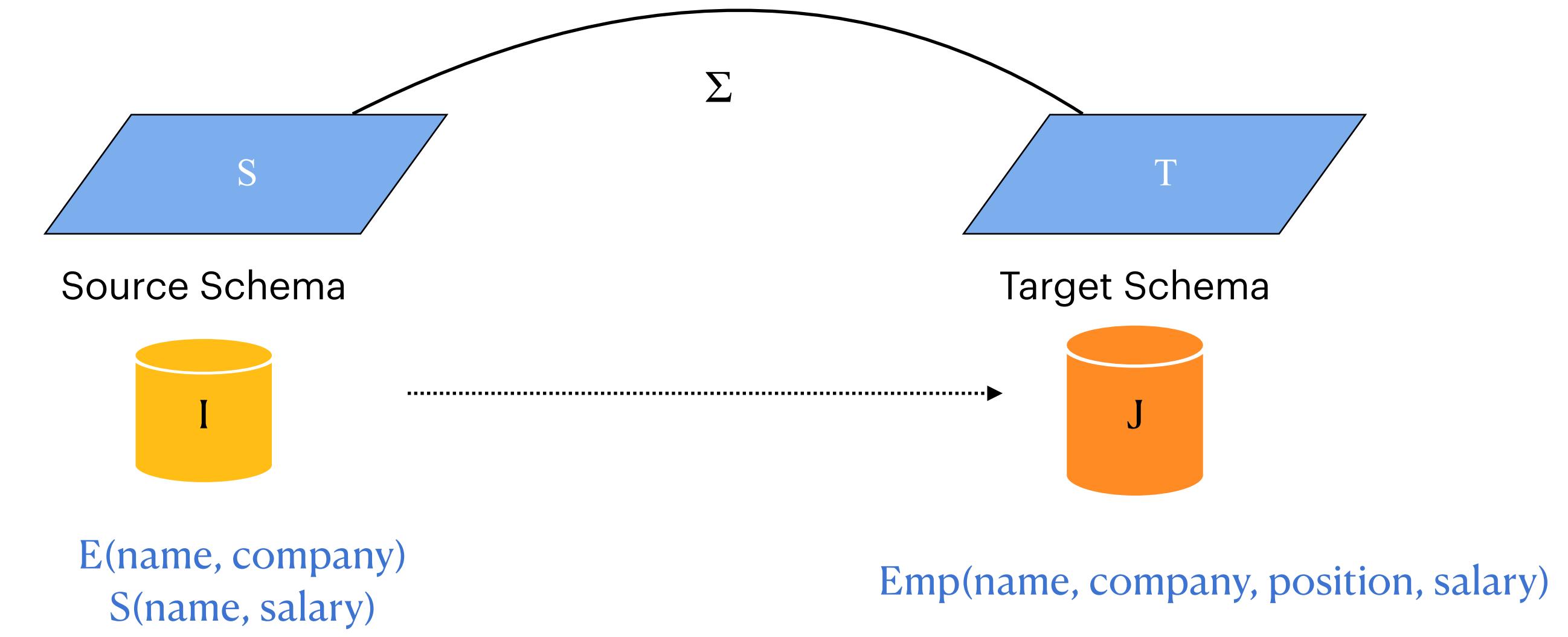
- Relational **source** schema  $\mathbf{S}$ , Relational **target** schema  $\mathbf{T}$
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**Constraints:**

- source-to-target tuple-generating dependencies (s-t tgds)  

$$\forall \mathbf{x}(\phi(\mathbf{x}) \rightarrow \exists \mathbf{y}\psi(\mathbf{x}, \mathbf{y}))$$
- target equality-generating dependencies (target egds)  

$$\forall \mathbf{x}(\theta(\mathbf{x}) \rightarrow x_k = x_l)$$



**Example:**

$$(\text{s-t tgd}) \quad \forall n, c, p(E(n, c) \wedge P(n, p) \rightarrow \exists s \text{ } \text{Emp}(n, c, p, s))$$

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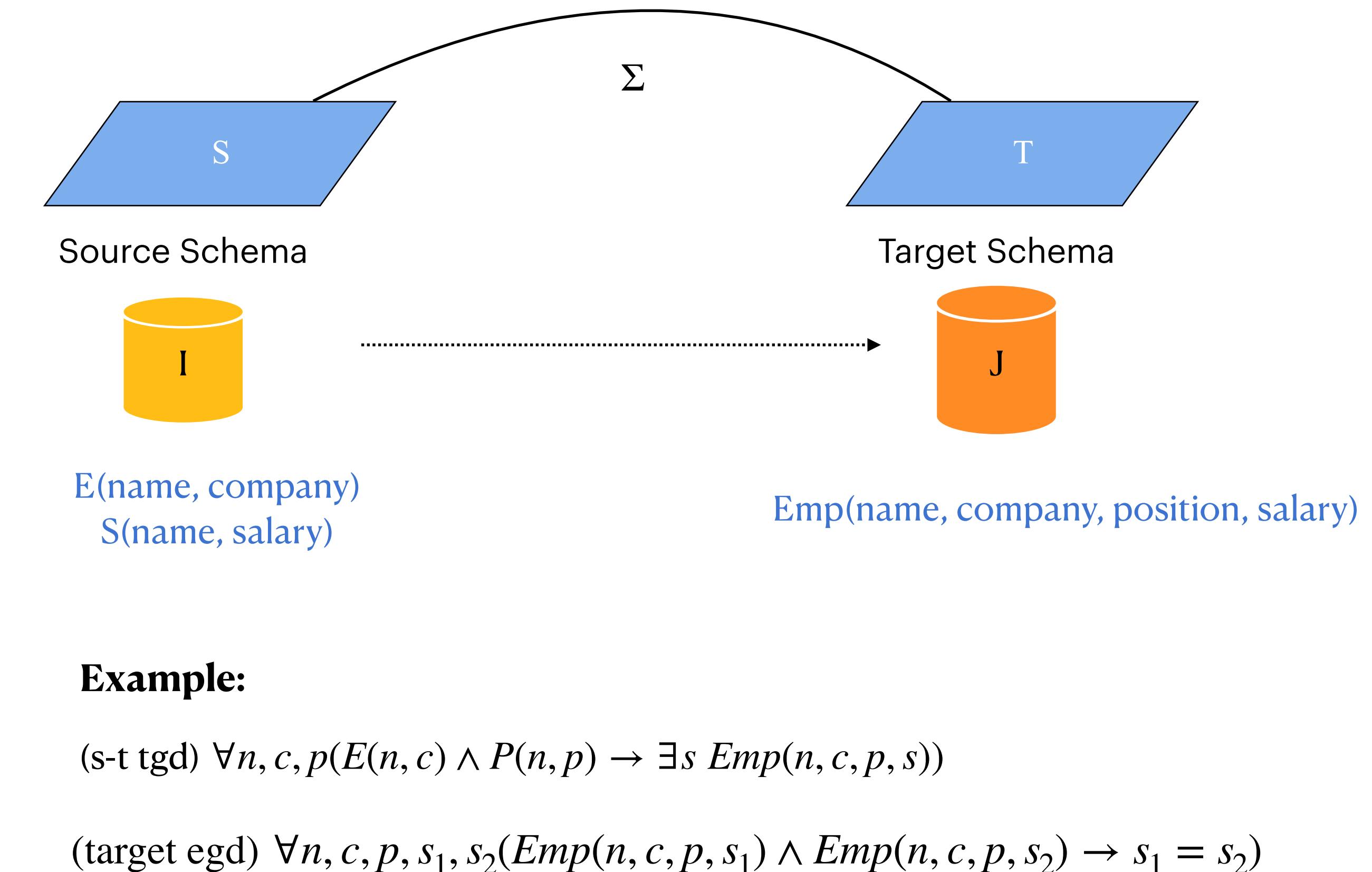
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**The data exchange problem:** given a source instance  $I$ , find a **solution** for  $I$ , that is, a target instance  $J$  such that the pair  $(I, J)$  satisfies the constraints  $\Sigma$  of  $\mathcal{M}$ .



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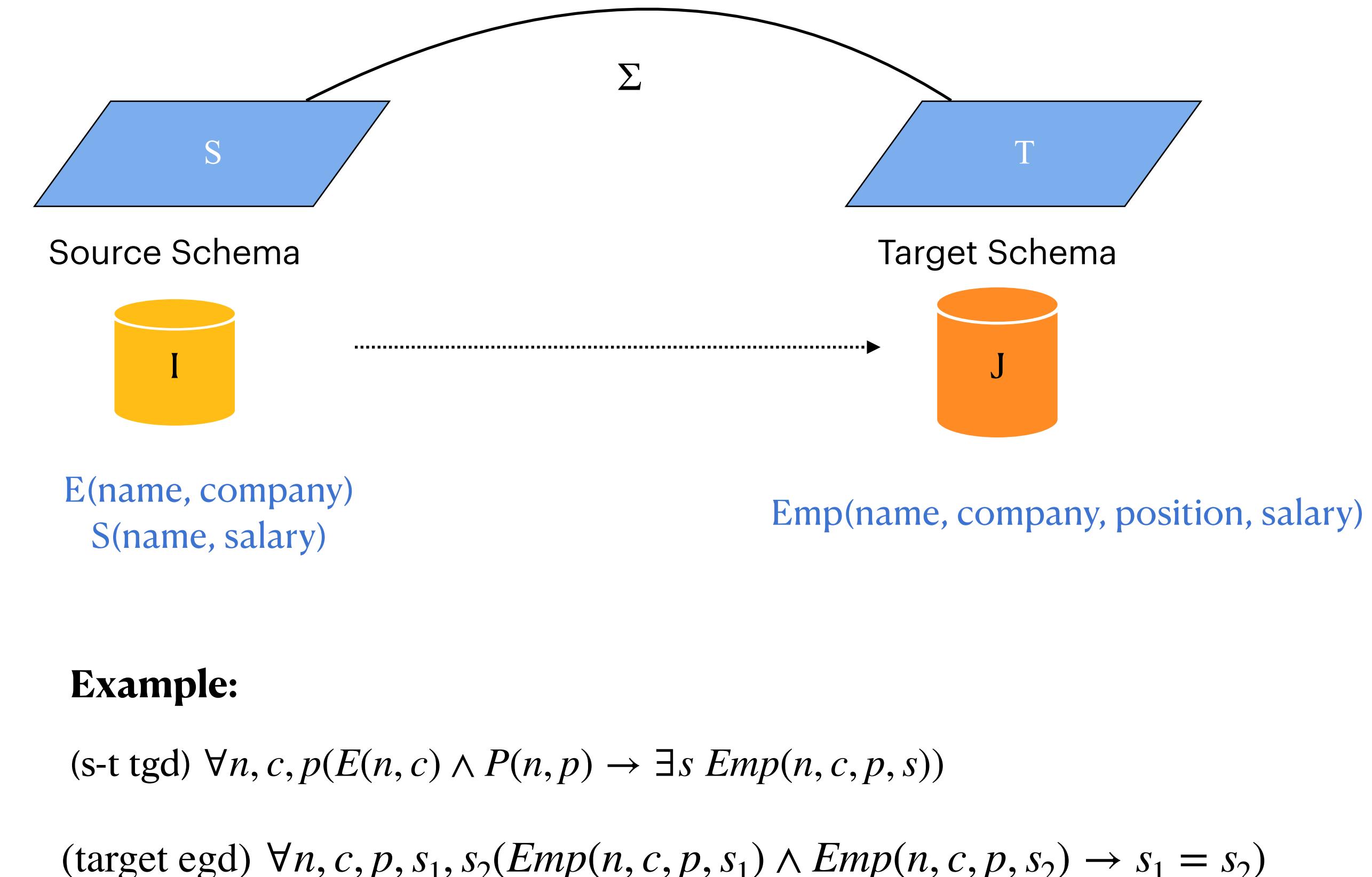
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**Universal Solutions:** The “most general” solutions (notion formalized using **homomorphisms**)



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# Temporal Databases

**Abstract Model of Time:** Time points (natural numbers)

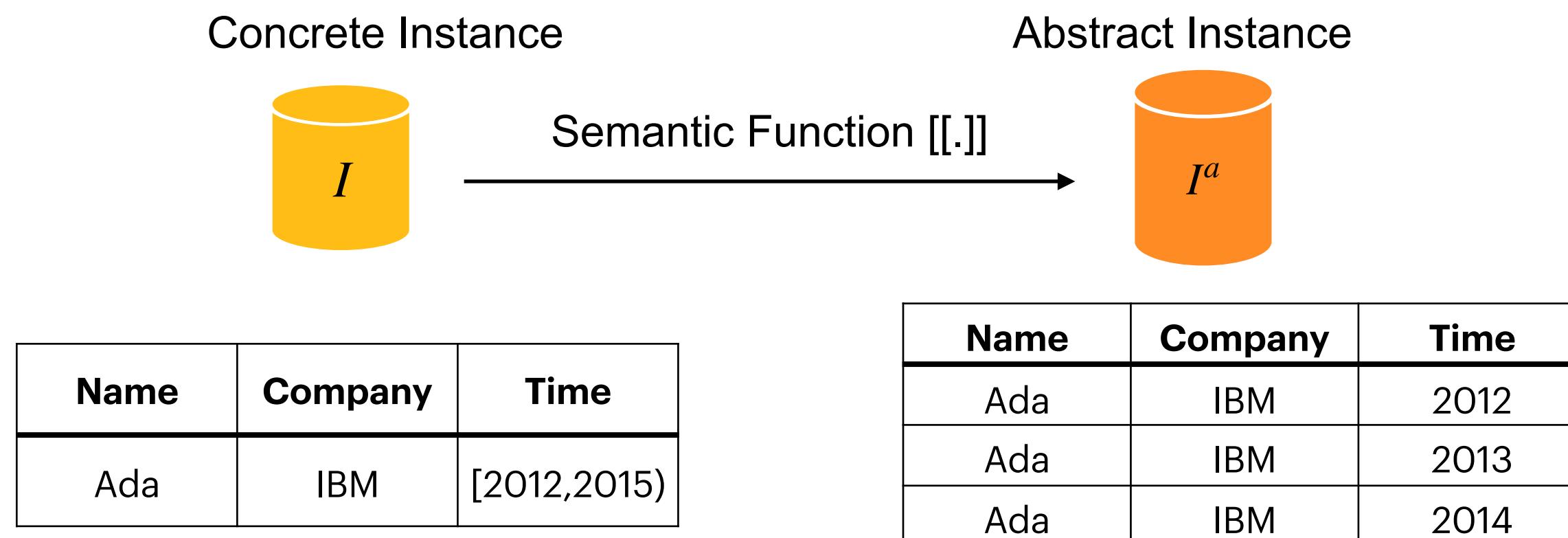
**Concrete Model of Time:** Time intervals (intervals  $[s, e]$ )

**Temporal Schema:** A schema with temporal relations, such as  $R(\text{Name}, \text{Company}, \text{Time})$

**Abstract Instance:** temporal attributes range over time points.

**Concrete Instance:** temporal attributes range over time intervals.

**Semantic Function  $[[\cdot]]$ :** convert all tuples of the form  $\mu = (c_1, \dots, c_m, [s, e])$  into  $[[\mu]] = \{(c_1, \dots, c_m, t) : s \leq t < e\}$ .



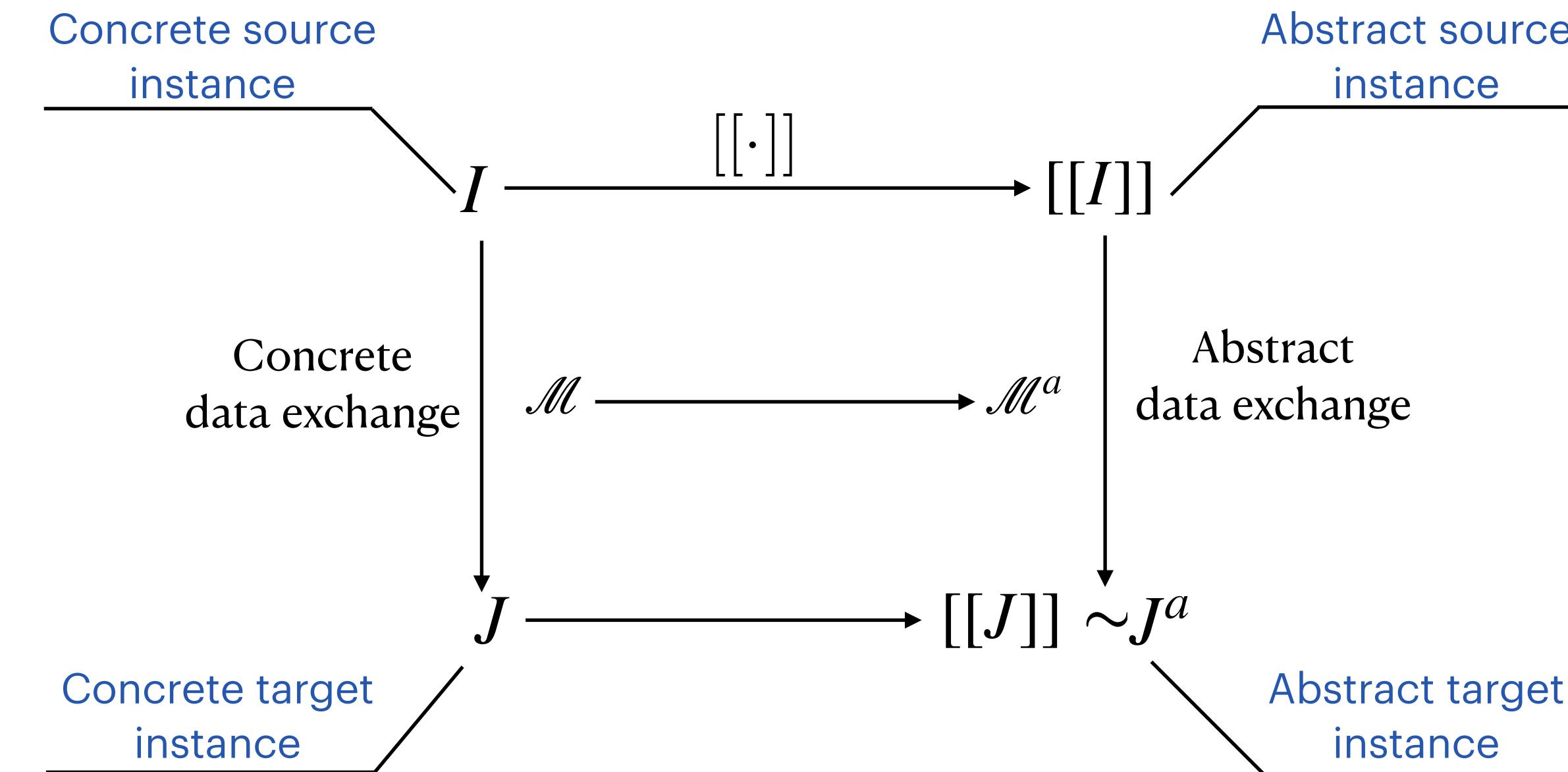
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**Temporal s-t tgds**  
 $\forall x, t(\phi(x, t) \rightarrow \exists y \psi(x, y, t))$

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**Semantic Adequacy:** Let  $I$  be a concrete source instance. We say that a concrete target instance  $J$  is **semantically adequate** for  $I$  if the abstract target instance  $[[J]]$  is a universal solution for  $[[I]]$  w.r.t.  $\mathcal{M}^a$ .

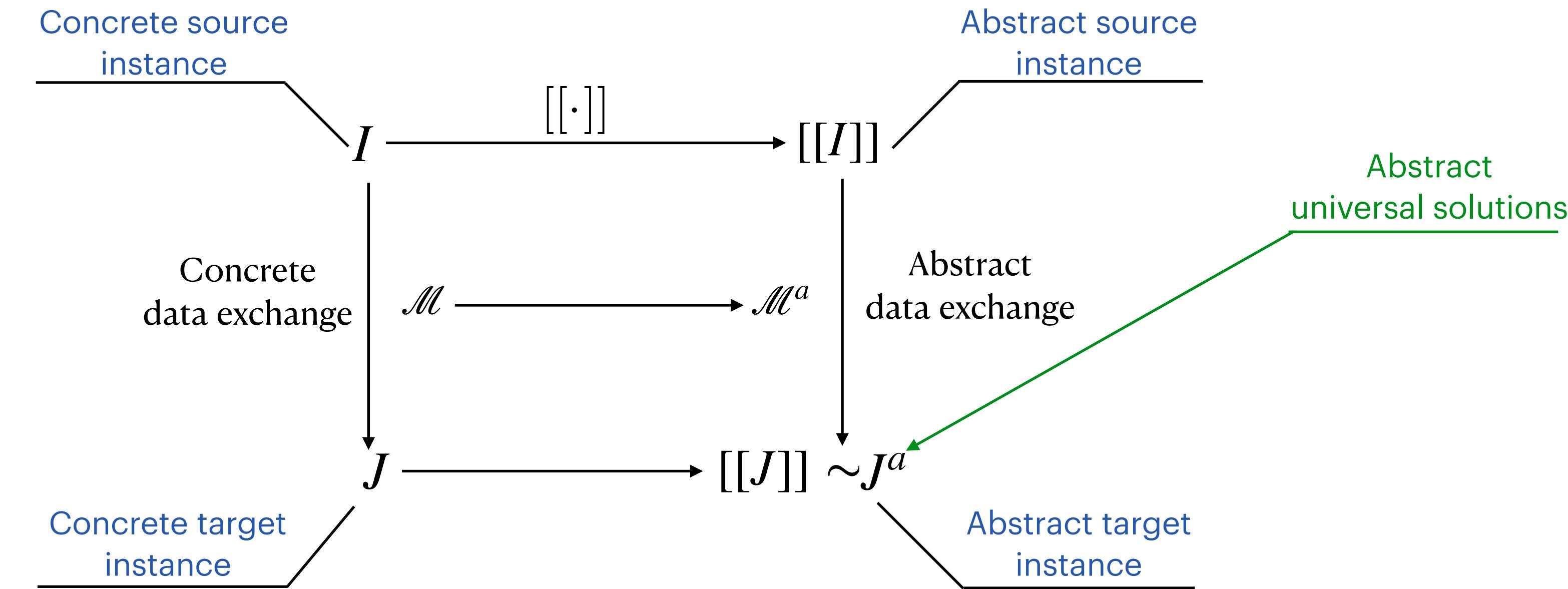
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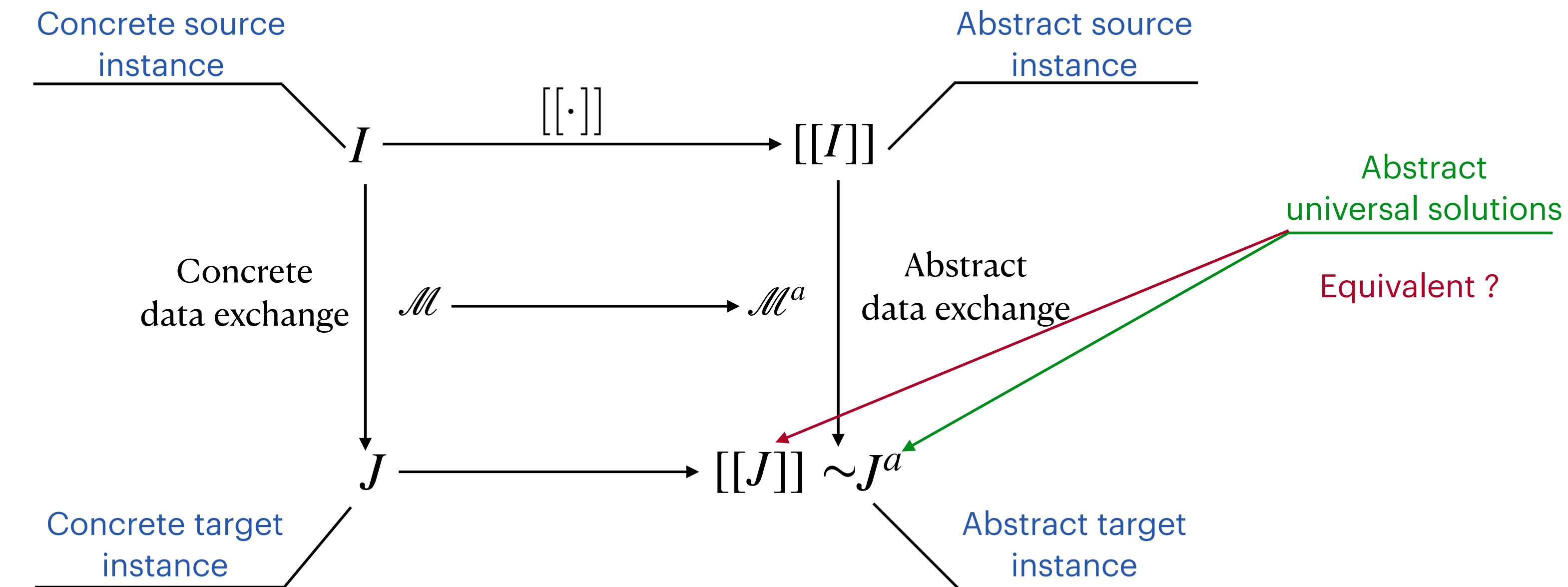
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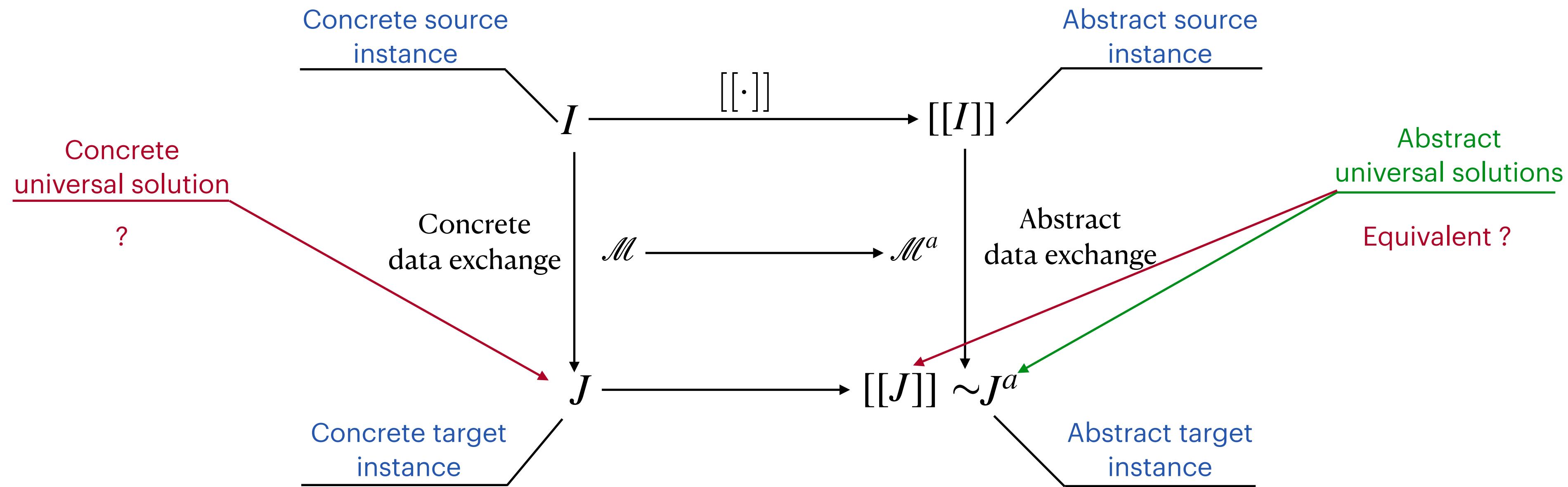
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# Challenges in Temporal Data Exchange

- In data exchange, universal solutions are produced using the chase algorithm which introduce **labelled nulls**  $N_j$  to witness  $\exists \mathbf{y}$  in  $\forall \mathbf{x}(\phi(\mathbf{x}) \rightarrow \exists \mathbf{y}\psi(\mathbf{x}, \mathbf{y}))$ .
- In **temporal** data exchange, **time-stamped nulls**  $N_j^t$  need to be introduced to witness  $\exists \mathbf{y}$  in  $\forall \mathbf{x}, t(\phi(\mathbf{x}, t) \rightarrow \exists \mathbf{y}\psi(\mathbf{x}, \mathbf{y}, t))$
- Managing time-stamped nulls requires special care when it comes to target constraints  
 $\forall \mathbf{x}, t(\theta(\mathbf{x}, t) \rightarrow x_k = x_l)$
- This becomes a challenging problem when multiple temporal variables are used in tgds.

# Temporal Data Exchange: Single Temporal Variable

Golshanara, L. and Chomicki, J.: Temporal data exchange. Inf. Syst. 87 (2020)

Considered **temporal schema mappings**  $\mathcal{M} = (\mathbf{S}, \mathbf{T}, \Sigma_{st}, \Sigma_t)$ , in which

- Every relation symbol in  $\mathbf{S}$  and  $\mathbf{T}$  has one temporal attribute
- Each constraint in  $\Sigma_{st} \cup \Sigma_t$  contains exactly one temporal variable
- Hence, the only temporal variable occurs in every atom of the consequent of s-t tgd; no temporal variable is existentially quantified.

**Example:**

<b>S</b>	<b>T</b>
E(name, company, time)	Emp(name, company, position, salary, time)
S(name, salary, time)	

**(s-t tgd)**  $\forall n, c, p, t(E(n, c, t) \wedge P(n, p, t) \rightarrow \exists s \ Emp(n, c, p, s, t))$

**(target egd)**  $\forall n, c, p, s_1, s_2, t(Emp(n, c, p, s_1, t) \wedge Emp(n, c, p, s_2, t) \rightarrow s_1 = s_2)$

**Theorem.** Let  $\mathcal{M}$  be a temporal schema mapping as above. There is a polynomial-time algorithm such that, given a concrete source instance  $I$ ,

- if a solution for  $[[I]]$  exists, then the algorithm produces a semantically adequate concrete target instance  $J$  for  $I$  w.r.t.  $\mathcal{M}$ .
- if there is no solution for  $[[I]]$ , then the algorithm fails.

**Note:** They did not address the question of whether there is always a concrete universal solution that is semantically adequate for  $I$ .

# Temporal Data Exchange: Single Temporal Variable

**Theorem 1.** There are

- a temporal schema mapping  $\mathcal{M}^* = (\mathbf{S}, \mathbf{T}, \Sigma_{st}^*, \Sigma_t^*)$  with one temporal variable in each constraint in  $\Sigma_{st}^* \cup \Sigma_t^*$ ,

and

- a concrete source instance  $I^*$ ,

such that

- there is a concrete universal solution for  $I^*$  w.r.t.  $\mathcal{M}^*$ , but [no concrete universal solution](#) is semantically adequate for  $I^*$ ;
- there is a concrete universal solution for  $\mathcal{N}(I^*)$  w.r.t.  $\mathcal{M}^*$ , but [no concrete universal solution](#) is semantically adequate for  $\mathcal{N}(I^*)$ .

( $\mathcal{N}(I^*)$  is a [normalized](#) version of  $I^*$ , computed in the first step of Golshanara & Chomicki's algorithm)

**Hint of proof.**

Schema mapping  $\mathcal{M}^*$

$$\text{s-t tgd: } \forall n, s, c, t(E(n, c, t) \wedge S(n, s, t) \rightarrow Emp(n, c, s, t))$$

$$\text{s-t tgd: } \forall n, c, p, t(P(n, p, t) \rightarrow \exists c EmpPos(n, c, p, t))$$

$$\text{target egd: } \forall n, c_1, c_2, s, p, t(\underbrace{Emp(n, c_1, s, t)}_{\text{underlined}} \wedge \underbrace{EmpPos(n, c_2, p, t)}_{\text{underlined}} \rightarrow c_1 = c_2)$$

Source instance  $I^*$

(a)  $E$

Name	Company	Time
Ada	IBM	[2013, 2018)
Bob	IBM	[2012, 2015)

(b)  $S$

Name	Salary	Time
Ada	18000	[2014, 2018)
Bob	13000	[2013, 2015)

(c)  $P$

Name	Position	Time
Ada	Manager	[2015, 2017)
Bob	Consultant	[2012, 2015)

# Temporal Data Exchange: Single Temporal Variable

**Theorem 2.** Let  $\mathcal{M} = (\mathbf{S}, \mathbf{T}, \Sigma_{st}, \Sigma_t)$  be a temporal schema mapping such that

- (a) each s-t tgd contains **at most one** temporal variable;
- (b) if an s-t tgd contains a temporal variable, then that temporal variable occurs in **every atom** of its consequent;
- (c) each target egd contains **at most one** temporal atom in its antecedent (it may contain non-temporal atoms).

There is a version of chase algorithm such that, given a concrete source instance  $I$ ,

- if a solution for  $\mathcal{N}(I)$  exists, then the algorithm produces a **semantically adequate concrete universal solution** for  $\mathcal{N}(I)$ ;
- if the algorithm fails, then there is no solution for  $[[I]]$  (note  $[[I]] = [[\mathcal{N}(I)]]$ ).

# Temporal Data Exchange: Multiple Temporal Variables

**Allen's relations on time intervals:** m (meets), o (overlaps), <(before), > (after) , and =(equals).

For instance, [2010, 2013) o [2011, 2014)

**Concrete s-t tgds**  $\forall \mathbf{x}, \mathbf{t} (\phi(\mathbf{x}, \mathbf{t}) \wedge \pi(\mathbf{t}) \rightarrow \exists \mathbf{y} \psi(\mathbf{x}, \mathbf{y}, \mathbf{t}))$

**Concrete target egds**  $\forall \mathbf{x}, \mathbf{t} (\theta(\mathbf{x}, \mathbf{t}) \wedge \rho(\mathbf{t}) \rightarrow x_k = x_l)$

**Theorem 3.** Let  $\mathcal{M} = (\mathbf{S}, \mathbf{T}, \Sigma_{st}, \Sigma_t)$  be a concrete schema mapping such that each s-t tgd is **full** and each target egd contains at most one temporal atom. There is a polynomial-time algorithm such that given a concrete source instance  $I$ ,

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**Concrete target egds**  $\forall \mathbf{x}, \mathbf{t} (\theta(\mathbf{x}, \mathbf{t}) \wedge \rho(\mathbf{t}) \rightarrow x_k = x_l)$

(full s-t tgd)  $\forall x_1, x_2, x_3, x_4, t_1, t_2 (R_2(x_1, x_2, x_3, t_1) \wedge R_3(x_1, x_4, t_2) \wedge (t_2 \text{ m } t_1) \rightarrow T_2(x_1, x_3, t_2))$

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# Concluding Remarks

- We showed that **semantically adequate universal solutions** may **not exist** even for temporal schema mappings with single temporal variable.
- We identified classes of schema mappings with **single temporal atom** in each target egd, for which semantically adequate universal solutions exist.
- We expanded the original framework of temporal data exchange studied by Golshanara and Chomicki via considering temporal schema mappings **with multiple temporal variables**.
- **Important Open Problem:** Study temporal schema mappings with existentially quantified temporal variables.

**Thank you for your attention**